



# MASTER IN PHOTONICS – PHOTONICS BCN EUROPHOTONICS-POESII MASTER COURSE

## PROPOSAL FOR A MASTER THESIS

**Dates: April - September 2017**

**Laboratory : QOT**

**Institution: ICFO**

**City, Country : Casteldefels (ES)**

**Title of the master thesis: *Simulating Cosmological models in optical lattices***

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### **Summary of the subject (maximum 1 page) :**

In this thesis, we propose to study the evolution of a gas of relativistic Dirac fermions in time dependent metrics in two spatial dimensions. The simplest example of the latter (Friedman-Lemaître-Robertson-Walker metric) describes the expansion or the collapse of a homogeneous and isotropous universe. If the gas is not interacting the model can be studied analytically as it is described in terms of a time-dependent single particle Dirac Hamiltonian  $H(t)$ .

The goal is to investigate the lattice version of this Hamiltonian, which is a generalized Hubbard model, and can be thought as a deformation of artificial graphene [1]. As in real graphene, relativistic Dirac fermions are emerging low-energy excitons around the Dirac points, namely cone like singularities of the energy bands.

The main tasks will be

- To find the appropriate choice of the coordinate frame and the simplest lattice formulation of  $H(t)$  that are suitable to be implemented within the scheme and setup proposed in [2] and [3], respectively;
- To consider the continuum limit of the lattice model and the role of lattice doubling in cosmological evolution;
- To define suitable observables that describe interesting phenomena like the “particle creation” and cosmological horizon;

- To compare the results for fermions with respect with the one obtained in analogue models of cosmological expansions with bosons, namely Bogoliubov excitations in a Bose-Einstein condensate, e.g. *cf.* [4]

[1] L.Tarruell *et al.*, “*Creating, moving and merging Dirac points with a Fermi gas in a tunable honeycomb lattice*”, *Nature* 483 (7389), 302-305 (2012).

[2] O. Boada, A. Celi, J.I. Latorre, and M. Lewenstein, “*Dirac equation for cold atoms in artificial curved spacetimes*”, *New J. Phys.* 13 (3), 035002, (2011).

[3] J. Rodriguez-Laguna, L. Tarruell, M. Lewenstein, and A. Celi, “*Synthetic Unruh effect in cold atoms*”, arXiv:1606.09505.

[4] C. Barceló, S. Liberati, and M. Visser, “*Living Rev. Relativity*”, 8, 12 (2005).  
<http://relativity.livingreviews.org/Articles/lrr-2011-3/>

**Keywords : Quantum Simulation, Ultracold atoms, optical lattices, artificial graphene, Quantum field theory in curved spacetime**

**Additional information :**

- \* Required skills: quantum mechanics; basic notion of special relativity and band theory;
- \* Miscellaneous: